## Recent progress in B physics

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## Outlines

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- $\mathrm{B} \rightarrow \pi \pi, \mathrm{K} \pi$
- Mixing-induced CP in $b \rightarrow$ s penguin
- $\mathrm{B}_{\mathrm{s}}-\mathrm{B}_{\mathrm{s}}$ bar mixing
- $\mathrm{B} \rightarrow$ VV polarizations
- Conclusion


## Introduction

- B physics has entered the era of precision measurement.
- Both theoretical and experimental precisions are improved.
- Discrepancies are observed. Critical examination is necessary for revealing new physics signals.


## Apology

- no inclusive B decays (Wu's talk at the previous meeting).
- No semileptonic B decays (Huang, Li, Qiao...)
- no B decays into charmonia (Chao...).
- No B decays into baryons (He, Li,...)
- no $\mathrm{B}_{\mathrm{c}}$ decays (Du, Lu, Zhang, Li, Ma, Li...)
- no new physics in B decays (Xiao, Yang, Wu...)


## Theories

## QCD-improved Factorization

(Beneke, Buchalla, Neubert, Sachrajda)

## Perturbative QCD

(Keum, Li, Sanda)
Soft-collinear Effective Theory
(Bauer, Pirjol, Rothstein, Stewart)
All assume large $m_{b}$

## QCDF

- Based on collinear factorization (Brodsky and Lepage 80).
- Compute correction to naïve factorization (NF), ie., the heavy-quark limit.

- Divergent like $\int_{0}{ }^{1} \mathrm{dx} / \mathrm{x}$ (end-point singularity) in collinear factorization


## Factorization formula

- $A\left(B \rightarrow M_{1} M_{2}\right)=\left(T^{\mid *} F^{\left.B M_{1}+T^{\| *} \phi_{B}{ }^{*} \phi_{M_{1}}\right)^{*} \phi_{M_{2}}}\right.$
- $T^{\prime}$ comes from vertex corrections, $\mathrm{O}\left(\alpha_{\mathrm{s}}\right)$


Magnetic penguin $\mathrm{O}_{89}$

- $\mathrm{T}^{\prime \prime}$ comes from spectator diagrams, $\mathrm{O}\left(\alpha_{\mathrm{s}}\right)$



## End-point singularity

- Singularity appears at $\mathrm{O}\left(1 / m_{b}\right)$, twist-3 spectator and annihilation amplitudes, parameterized as $X=\left(1+\rho e^{i \phi}\right) \ln \left(m_{b} / \Lambda\right)$

- For QCDF to be predictive, $\mathrm{O}\left(1 / \mathrm{m}_{\mathrm{b}}\right)$ corrections are better to be small $\approx$ FA.
- Data show important $\mathrm{O}\left(1 / \mathrm{m}_{\mathrm{b}}\right)$. Different free $(\rho, \phi)$ must be chosen for $B \rightarrow P P, P V, V P$.


## $\mathrm{O}\left(\alpha_{s}{ }^{2}\right)$ corrections

- b $\rightarrow \mathrm{d}(\mathrm{s}) \mathrm{g}^{*} \mathrm{~g}^{*}(\mathrm{Li}$, Yang 05, 06)
- Enhance penguin and rates of penguindominated modes, such as $B \rightarrow \pi K$, but....
- Minor effects on tree-dominated modes, such as $B \rightarrow \pi \pi$.
- Incomplete $\mathrm{O}\left(\alpha_{c}{ }^{2}\right)$ for $\mathrm{T}^{\text {II }}$.



## QCDF/SCET---complete $O\left(\alpha_{s}{ }^{2}\right) T^{\prime \prime}$



- Motivated by $\mathrm{B} \rightarrow \pi \pi$ data:
- O( $\alpha_{s}{ }^{2}$ ) for J, major effect (Beneke, Yang 05)
- $\mathrm{O}\left(\alpha_{s}{ }^{2}\right)$ for $\mathrm{H}^{\prime \prime}$ (Beneke, Jager 05)
- $\mathrm{O}\left(\alpha_{s}{ }^{2}\right)$ for $\mathrm{H}^{\text {II }}$ of penguin amplitudes (BJ 06).

- Enhance color-suppressed tree, not QCD penguin


## PQCD

- End-point singularity means breakdown of collinear factorization
- Use more "conservative" $k_{T}$ factorization (Li and Sterman 92)
- Parton $\mathrm{k}_{\mathrm{T}}$ smear the singularity

$$
\int_{0}^{1} d x \frac{1}{x+k_{T}^{2} / m_{B}^{2}}
$$

- Same singularity in form factor is also smeared
- No free parameters



## Factorization picture



## Sudakov factors S,

 summation of $\alpha_{s} \ln ^{2}\left(m_{b} / k_{T}\right)$ to all orders, describe parton distribution in $\mathrm{k}_{\mathrm{T}}$PQCD picture for two-body nonleptonic decays. Always collinear gluons

Large $\mathrm{k}_{\mathrm{T}}$ Small b
$k_{T}$ accumulates after infinitely many gluon exchanges, similar to DGLAP evolution up to $\mathrm{k}_{\mathrm{T}} \sim \mathrm{Q}$
$\mathrm{O}\left(\alpha_{s}{ }^{2}\right)$ corrections (Li, Mishima, Sanda 05)

- LO: all pieces at LO
- $\mathrm{LO}_{\text {nlowc: }}$ NLO Wilson coefficients
- VC: vertex correction
- QL: quark loops
- MP: Magnetic penguin $\}$ decrease $P$ by $10 \%$


- Corrections to form factors are nontrivial (Ma, Wang 04; 06).


## SCET

- Two scales in B decays: $m_{b} \Lambda$ and $m_{b}{ }^{2}$
- Full theory $\rightarrow$ SCET $_{1}$ : integrate out the lines off-shell by $\mathrm{m}_{\mathrm{b}}{ }^{2}$



## SCET $_{\|}$

- SCET $_{1} \rightarrow$ SCET $_{11}$ : integrate out the lines off-shell by $\mathrm{m}_{\mathrm{b}} \Lambda$

- Compared to QCDF, $\mathrm{T}^{\prime \prime} \rightarrow \mathrm{T}\left(\mu_{0}\right) \mathrm{J}\left(\mu_{0}, \mu\right)$
- Framework for $\mathrm{O}\left(\alpha_{s}{ }^{2}\right)$ QCDF/SCET.


## BPRS's SCET

- Do not attempt to calculate matrix elements in SCET, but treat them as free parameters determined by data (Bauer, Pirjol, Rothstein, Stewart 04).
- Even introduce arbitrary charming penguins in order to input strong phases.
- BPRS's SCET is not very different from amplitude parameterization using SU(3).
- Intensive application by Williamson, Zupan 06.


## Zero-bin subtraction (Manohar, Stewart 06)

- Effective theory with more than two momenta, IR modes are doubly counted.
- $P_{1}=0$ bin should be removed

- Form factor is factorizable
- Merge with PQCD


Soft quark absorbed into $\phi_{\mathrm{B}} \quad$ energetic

## Higher-power corrections are not yet explored!

A much more difficult job

## Phenomenology

## $\mathrm{B} \rightarrow \pi \pi, \mathrm{K} \pi$

## Naïve power counting

- Estimate order of magnitude of B decay amplitudes in power of the Wolfenstein parameter $\lambda \sim 0.22$
- It is not a power counting from any rigorous theory
- Amplitude~ (CKM) (Wilson coefficient)

- CKM matrix elements

$$
|\rho-i \eta| \approx 0.4
$$

$\begin{aligned} &\left(\begin{array}{ccc}V_{u d} & V_{u s} & V_{u b} \\ V_{c d} & V_{c s} & V_{c b} \\ V_{t d} & V_{t s} & V_{t b}\end{array}\right)=\left(\begin{array}{ccc}1-\frac{\lambda^{2}}{2} & \lambda & A \lambda^{3}(\rho-i \eta) \\ -\lambda & 1-\frac{\lambda^{2}}{2} & A \lambda^{2} \\ A \lambda^{3}(1-\rho-i \eta) & -A \lambda^{2} & 1\end{array}\right) \\ &=\left(\begin{array}{ccc}O(1) & O(\lambda) & O\left(\lambda^{4}\right) \\ O(\lambda) & O(1) & O\left(\lambda^{2}\right) \\ O\left(\lambda^{3}\right) & O\left(\lambda^{2}\right) & O(1)\end{array}\right), \\ & O(1): a_{1},\end{aligned}$

- Wilson coefficients $O(\lambda): a_{2}, 1 / N_{c}$

$$
\begin{aligned}
& \mathrm{a}_{1}=\mathrm{C}_{2}+\mathrm{C}_{1} / \mathrm{N}_{\mathrm{c}} \\
& \mathrm{a}_{2}=\mathrm{C}_{1}+\mathrm{C}_{2} / \mathrm{N}_{\mathrm{c}}
\end{aligned}
$$

$$
O\left(\lambda^{2}\right): C_{4}, C_{6}, a_{4}, a_{6}
$$

$$
O\left(\lambda^{3}\right): C_{3}, C_{5}, C_{9}, a_{3}, a_{5}, a_{9}
$$

$$
O\left(\lambda^{4}\right): C_{10},
$$

$$
O\left(\lambda^{5}\right): C_{7}, C_{8}, a_{7}, a_{8}, a_{10}
$$

## Quark amplitudes

 most recent work by Wu, Zhou, Zhuang

Color-allowed tree T
Color-suppressed tree C


QCD penguin $P$
Electroweak penguin $\mathrm{P}_{\mathrm{ew}}$

## $\pi \pi$ parametrization

$$
\begin{aligned}
\sqrt{2} A\left(B^{+} \rightarrow \pi^{+} \pi^{0}\right) & =-T\left[1+\frac{C}{T}+\frac{P_{e w}}{T} e^{i \phi_{2}}\right] \\
A\left(B_{d}^{0} \rightarrow \pi^{+} \pi^{-}\right) & =-T\left(1+\frac{P}{T} e^{i \phi_{2}}\right) \\
\sqrt{2} A\left(B_{d}^{0} \rightarrow \pi^{0} \pi^{0}\right) & =T\left[\left(\frac{P}{T}-\frac{P_{e w}}{T}\right) e^{i \phi_{2}}-\frac{C}{T}\right]
\end{aligned}
$$

$\lambda \approx 0.2 \quad \frac{P}{T} \sim \lambda, \quad \frac{C}{T} \sim \lambda, \quad \frac{P_{e w}}{T} \sim \lambda^{2} . \quad$ Treedominant $\left(\mathrm{C}_{4} / \mathrm{C}_{2}\right)\left(\mathrm{V}_{\mathrm{td}} \mathrm{V}_{\mathrm{tb}} / \mathrm{V}_{\mathrm{ud}} \mathrm{V}_{\mathrm{ub}}\right) / 1 \sim\left(\lambda^{2} / 1\right)\left(\lambda^{3} / \lambda^{4}\right) \sim \lambda$

## $\mathrm{B} \rightarrow \pi \pi$ puzzle

- $P, C$, and $P_{e w}$ in $\pi^{0} \pi^{0}$ are all subleading.
- We should have $\operatorname{Br}\left(\pi^{0} \pi^{0}\right) \approx \mathrm{O}\left(\lambda^{2}\right) \operatorname{Br}\left(\pi^{+} \pi^{-}\right)$
- Data show $\operatorname{Br}\left(\pi^{0} \pi^{0}\right) \approx \mathrm{O}(\lambda) \operatorname{Br}\left(\pi^{+} \pi^{-}\right)$

$$
\begin{array}{ll}
\mathrm{B}(\mathrm{BO} \rightarrow \pi+\pi-)=(5.2 \pm 0.2) \times 10^{-6} & \\
\mathrm{~B}(\mathrm{~B}+\rightarrow \pi+\pi 0)=(5.7 \pm 0.4) \times 10^{-6} & \text { reduced } \mathrm{f} \\
\mathrm{~B}(\mathrm{BO} \rightarrow \pi 0 \pi 0)=(1.3 \pm 0.2) \times 10^{-6} \longleftarrow & 1.5 \times 10^{-6}
\end{array}
$$

- Large P and/or C---motivates $\mathrm{O}\left(\alpha_{\mathrm{s}}{ }^{2}\right)$ QCDF/SCET. It remains as a puzzle, because $B\left(\rho^{0} \rho^{0}\right)=(1.16 \pm 0.46) \times 10^{-6}(\mathrm{Li}$, Mishima 06).


## $K \pi$ parameterization

$$
\begin{aligned}
& A\left(B^{+} \rightarrow K^{0} \pi^{+}\right)=P^{\prime}, \\
& A\left(B_{d}^{0} \rightarrow K^{+} \pi^{-}\right)=-P^{\prime}\left(1+\frac{T^{\prime}}{P^{\prime}} e^{i \phi_{3}}\right), \\
& \sqrt{2} A\left(B^{+} \rightarrow K^{+} \pi^{0}\right)=-P^{\prime}\left[1+\frac{P_{e w}^{\prime}}{P^{\prime}}+\left(\frac{T^{\prime}}{P^{\prime}}+\frac{C^{\prime}}{P^{\prime}}\right) e^{i \phi_{3}}\right], \\
& \sqrt{2} A\left(B_{d}^{0} \rightarrow K^{0} \pi^{0}\right)=P^{\prime}\left(1-\frac{P_{e w}^{\prime}}{P^{\prime}}-\frac{C^{\prime}}{P^{\prime}} e^{i \phi_{3}}\right), \\
& \frac{T^{\prime}}{P^{\prime}} \sim \lambda, \quad \frac{P_{e w}^{\prime}}{P^{\prime}} \sim \lambda, \quad \frac{C^{\prime}}{P^{\prime}} \sim \lambda^{2} \\
&\left(\mathrm{C}_{2} / \mathrm{C}_{4}\right)\left(\mathrm{V}_{\mathrm{us}} \vee_{\mathrm{ub}} / \mathrm{V}_{\mathrm{ts}} \mathrm{~V}_{\mathrm{tb}}\right) \sim\left(1 / \lambda^{2}\right)\left(\lambda^{5} / \lambda^{2}\right) \sim \lambda
\end{aligned}
$$

## Direct CP in $\mathrm{B} \rightarrow \mathrm{K} \pi$

- $\mathrm{K}^{+} \pi^{-}$and $\mathrm{K}^{+} \pi^{0}$ differ by subleading amplitudes, $\mathrm{P}_{\mathrm{ew}} / \mathrm{P} \sim \mathrm{C} / \mathrm{T} \sim \lambda$. Their $\subset P$ are expected to be similar.

$$
\begin{aligned}
A_{C P}^{0} & =\frac{\operatorname{Br}\left(\bar{B}_{d}^{0} \rightarrow K^{-} \pi^{+}\right)-\operatorname{Br}\left(B_{d}^{0} \rightarrow K^{+} \pi^{-}\right)}{\operatorname{Br}\left(\bar{B}_{d}^{0} \rightarrow K^{-} \pi^{+}\right)+\operatorname{Br}\left(B_{d}^{0} \rightarrow K^{+} \pi^{-}\right)}, \\
A_{C P}^{\prime c} & =\frac{\operatorname{Br}\left(B^{-} \rightarrow K^{-} \pi^{0}\right)-\operatorname{Br}\left(B^{+} \rightarrow K^{+} \pi^{0}\right)}{\operatorname{Br}\left(B^{-} \rightarrow K^{-} \pi^{0}\right)+\operatorname{Br}\left(B^{+} \rightarrow K^{+} \pi^{0}\right)},
\end{aligned}
$$

- Their data differ by more than $3 \sigma$ !
- $A_{\text {CP }}\left(K^{+} \pi^{-}\right)=-(9.3 \pm 1.5) \%$
- $\mathrm{A}_{\mathrm{CP}}\left(\mathrm{K}^{+} \pi^{0}\right)=(4.7 \pm 2.6) \%$, large $\mathrm{P}_{\mathrm{ew}}$ or C ?
- $b \rightarrow s g^{*} g^{*}$, FSI can not resolve the puzzle.


## Large strong phase

- $\mathrm{A}_{\mathrm{CP}}\left(\mathrm{K}^{+} \pi^{-}\right) \approx-0.115$ implies sizable $\delta_{\mathrm{T}} \sim 15^{\circ}$ between T and P (Keum, Li, Sanda 00)



## Explanation 1

- How to understand the small $\mathrm{A}_{\mathrm{CP}}\left(\mathrm{K}^{+} \pi^{0}\right)$ ?
- Large $\mathrm{P}_{\mathrm{Ew}}$ to rotate P (Buras et al.; Yoshikawa; Gronau and Rosner; Ciuchini et al., Kundu and Nandi, Wu and Zhou)
- Also motivated by old large $B\left(K^{0} \pi^{0}\right)$ data $\Rightarrow$ new physics?



## Explanation 2

- Large C to rotate T (Charng and Li; He and McKellar)
$\Rightarrow$ mechanism missed in naïve power counting?
- $C$ is subleading by itself. Try NLO PQCD.



## Vertex correction

- Vertex correction enhances $\mathrm{C} \propto \mathrm{a}_{2}$, and makes it almost imaginary.



Without vertex correction

Re, with vertex correction Im, with vertex correction Is negative. It rotates T !

## PQCD results

| Mode | Data [1] | LO | LO ${ }_{\text {NLOWC }}$ | +VC | +QL | +MP | +NLO |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $B^{ \pm} \rightarrow \pi^{ \pm} K^{0}$ | $24.1 \pm 1.3$ | 17.3 | 32.9 | 31.6 | 34.9 | 24.5 | $24.9_{-8.2}^{+13.9}$ ( | (3.2) |
| $B^{ \pm} \rightarrow \pi^{0} K^{ \pm}$ | $12.1 \pm 0.8$ | 10.4 | 18.7 | 17.7 | 19.7 | 14.2 | $14.2_{-5.8}^{+10.2}$ |  |
| $B^{0} \rightarrow \pi^{\mp} K^{ \pm}$ | $18.9 \pm 0.7$ | 14.3 | 28.0 | 26.9 | 29.7 |  | $21.1{ }_{-8.4}^{+15.7}$ |  |
| $B^{0} \rightarrow \pi^{0} K^{0}$ | $11.5 \pm 1.0$ | 5.7 | 12.2 | 11.9 | 13.0 |  | 9.2-3.3 ${ }^{+5.6}$ | 2.01 |
| $B^{0} \rightarrow \pi^{\mp} \pi^{ \pm}$ | $5.0 \pm 0.4$ | 7.1 | 6.8 | 6.6 | 6.9 | 6.7 | $6.6{ }_{-3.8}^{+6.7}$ |  |
| $B^{ \pm} \rightarrow \pi^{ \pm} \pi^{0}$ | $5.5 \pm 0.6$ | 3.5 | 4.2 | 4.1 | 4.2 | 4.2 | $4.1+3.5\}$ |  |
| $B^{0} \rightarrow \pi^{0} \pi^{0}$ | $1.45 \pm 0.29$ | 0.12 | 0.28 | 0.37 | 0.29 | 0.21 | $0.30_{-0.21}^{+0.49}$ | (0.091 |


| Mode | Data [1] | LO | $\mathrm{LO}_{\text {NLOW }}$ | +VC | +Q | +MP | +NLO |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $B^{ \pm} \rightarrow \pi^{ \pm} K^{0}$ | $-0.02 \pm 0.04$ | -0.01 | -0.01 | -0.01 | 0.00 | -0.01 | $0.00 \pm 0.00( \pm 0.00)$ |
| $B^{ \pm} \rightarrow \pi^{0} K^{ \pm}$ | $0.04 \pm 0.04$ | -0.08 | -0.06 | -0.01 | -0.05 | -0.0 | $0.01_{-0.05}^{+0.03}(+0.05)$ |
| $B^{\circ} \rightarrow \pi^{\mp} K$ | 11 | -0.12 | 0.08 | -0.00 | -0.06 | -0.10 | $-0.09_{-0.08(+0.06)}^{+0.06}$ |
| $B^{0} \rightarrow \pi^{0} K^{0}$ |  | -0.02 | 0.00 | -0.07 | 0.00 | 0.00 | $-0.07_{-0.03}^{+0.03(+0.01)}$ |
| $B^{0} \rightarrow \pi^{\mp} \pi^{ \pm}$ | $0.37 \pm 0.10$ | 0.14 | 0.19 | 0.21 | 0.16 | 0.20 | $0.18_{-0.12(-0.06)}^{+0.20}(+0.07)$ |
| $B^{ \pm} \rightarrow \pi^{ \pm} \pi^{0}$ | $0.01 \pm 0.06$ | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | $0.00 \pm 0.00( \pm 0.00)$ |
| $B^{0} \rightarrow \pi^{0} \pi^{0}$ | $0.28{ }_{-0.39}^{+0.40}$ | -0.04 | -0.34 | 0.65 | -0.41 | -0.43 | $\begin{aligned} & 0.63_{-0.34(-0.15)}^{+0.35}(+0.09) \end{aligned}$ |

## QCDF

## $\delta_{\mathrm{T}}$ has a wrong sign in QCDF. C makes the

 situation worse.

## SCET

- C/T is real in leading SCET, and large from the $\pi \pi$ data.
- C can not reduce $\mathrm{A}_{\mathrm{CP}}\left(\mathrm{K}^{+} \pi^{0}\right)$ (hep-ph/0510241).



## Large $\mathrm{P}_{\mathrm{ew}}$ ?

- $\mathrm{A}_{\mathrm{CP}}\left(\mathrm{K}^{+} \pi^{-}\right)$is insensitive to NLO. NLO could modify C , and thus $\mathrm{A}_{\mathrm{CP}}\left(\mathrm{K}^{+} \pi^{0}\right)$. C remains subleading, and branching ratios do not change much.
- Predicted $B\left(\pi^{0} \mathrm{~K}^{0}\right)$ is smaller than old data.
$R_{n}=\frac{1}{2} \frac{B\left(B^{0} \rightarrow \pi^{\mp} K^{ \pm}\right)}{B\left(B^{0} \rightarrow \pi^{0} K^{0}\right)}=0.79 \pm 0.08$
- New data soften the need for large $P_{\text {ew }}$

PQCD (05)


Mixing-induced $\subset P^{\prime}$ in $b \rightarrow s$

## Calculation of the time-dependent CP asymmetry

$$
\begin{aligned}
A_{f_{C P}}(t) & =\frac{\left.\left.\left|\left\langle f_{C P}\right| H\right| \bar{B}^{0}(t)\right\rangle\left.\right|^{2}-\left|\left\langle f_{C P}\right| H\right| B^{0}(t)\right\rangle\left.\right|^{2}}{\left.\left.\left|\left\langle f_{C P}\right| H\right| \bar{B}^{0}(t)\right\rangle\left.\right|^{2}+\left|\left\langle f_{C P}\right| H\right| B^{0}(t)\right\rangle\left.\right|^{2}} \\
& =\frac{\Gamma\left(\bar{B}^{0}(t) \rightarrow f_{C P}\right)-\Gamma\left(B^{0}(t) \rightarrow f_{C P}\right)}{\Gamma\left(\bar{B}^{0}(t) \rightarrow f_{C P}\right)+\Gamma\left(B^{0}(t) \rightarrow f_{C P}\right)}
\end{aligned}
$$

$$
\begin{gathered}
A_{f_{C P}}(t)=S \cdot \sin (\Delta m \cdot t)-C \cdot \cos (\Delta m \cdot t) \\
S=\frac{2 \cdot \operatorname{Im}(\lambda)}{1+|\lambda|^{2}} \quad C=\frac{1-|\lambda|^{2}}{1+|\lambda|^{2}}
\end{gathered}
$$

1 decay amplitude:

$$
\begin{aligned}
|\lambda|=1 \quad \Rightarrow \quad S & =\operatorname{Im}(\lambda), \quad C=0 \\
A_{f_{C P}}(t) & =\operatorname{Im}(\lambda) \cdot \sin (\Delta m \cdot t)
\end{aligned}
$$

## Calculating $\lambda$



$$
\begin{aligned}
& B^{0} \rightarrow J / \psi K_{s}^{0} \quad \lambda=(-1) \cdot \frac{V_{t b}^{*} V_{t d}}{V_{t b} V_{t d}^{*}} \cdot \frac{V_{c s}^{*} V_{c b}}{V_{c s} V_{c b}^{*}} \cdot \frac{V_{c d}^{*} V_{c s}}{V_{c d} V_{c s}^{*}} \operatorname{Im}(\lambda)=\sin (2 \beta) \\
& (b \rightarrow c \overline{c s}) \times\left(K^{0} \rightarrow K_{s}^{0}\right)
\end{aligned} \prod_{\text {K-Kbar mixing }}
$$

## $\sin 2 \phi_{1} / \sin 2 \beta$

- 1 decay amplitude, $\lambda_{\mathrm{f}_{\mathrm{CP}}}=\exp \left(-2 \mathrm{i} \phi_{1}\right)$
- Measure $\mathrm{S}_{\mathrm{f} C P} \propto \operatorname{Im} \lambda_{\mathrm{f}_{\mathrm{CP}}} \Rightarrow$ measure $\sin \left(2 \phi_{1}\right)$
- Either pure-tree or pure-penguin modes serve the purpose
- Tree-dominant $\mathrm{B} \rightarrow \mathrm{J} / \psi \mathrm{K}_{\mathrm{S}}$, penguin pollution:

$$
\mathrm{P} / \mathrm{T} \sim\left(\mathrm{C}_{4} / \mathrm{C}_{2}\right)\left(\mathrm{V}_{\mathrm{us}} \mathrm{~V}_{\mathrm{ub}} / \mathrm{V}_{\mathrm{cs}} \mathrm{~V}_{\mathrm{cb}}\right) \sim \lambda^{4} \sim 0.2 \%
$$

- Penguin-dominant $\mathrm{b} \rightarrow \mathrm{s}$, tree pollution:

$$
\lambda_{\pi^{0} K_{S}}=-e^{-2 i \phi_{1}} \frac{P^{\prime}-P_{e w}^{\prime}-C^{\prime} e^{-i \phi \phi_{3}}}{P^{\prime}-P_{e w}^{\prime}-C^{\prime} e^{i \phi_{3}}} .
$$

$C^{\prime} / P^{\prime} \sim \lambda^{2} \sim 5 \%$

## $\sin \left(2 \beta^{\text {eff }}\right) / \sin \left(2 \phi_{1}^{\text {eff }}\right)$

LP 2005
PRELIMINARY


Penguin-dominated
$\Delta S \equiv " \sin 2 \phi_{1}^{\prime \prime}-\sin 2 \phi_{1}$

Tree-dominated
$\triangle S \neq 0$ by
about $1 \sigma$
A puzzle?
$\sin \left(2 \beta^{\text {eff }}\right) \equiv \sin \left(2 \phi_{1}^{\text {eff }}\right)$
PRELIMINARY


## $\Delta$ S puzzle is still there

## Recent theoretical calculation of $\Delta \mathrm{S}$

|  | QCDFFFSI <br> Cheng-Chua- <br> Soni | QCDF <br> Beneke | QCDF <br> Buchalla- <br> Hiller-Nir-Raz | SCET <br> Williamson-Zupan |
| :--- | :--- | :--- | :--- | :--- |
| $\Delta S(\phi \mathrm{Ks})$ | $0.03_{-0.04}^{+0.01}$ | $0.02 \pm 0.01$ | 0.02 | PQCD <br> Li, Mishima |
| $\Delta \mathrm{S}\left(\eta^{\prime} \mathrm{KS}\right)$ | $0.00_{-0.04}^{+0.00}$ |  |  |  | $0.03^{+0.01} \pm 0.01 ~ 0.01_{-0.01}^{+0.01}$

$\Delta S \propto \cos \delta_{\mathrm{C}}$, large C but $\delta_{\mathrm{C}} \approx 90^{\circ}$ in NLO PQCD
All approaches gave consistent results, and small uncertainty. Tree pollution remains small even with NLO. Promising new physics signal, if data persist.

## $B_{s}-B_{s}$ bar mixing

## $\Delta \mathrm{m}_{\mathrm{d}}$ and $\Delta \mathrm{m}_{\mathrm{s}}$ : constraints in the $(\rho-\eta)$ plane

$\Delta m_{s}=\frac{G_{F}^{2}}{6 \pi^{2}} m_{B_{s}} m_{W}^{2} \eta_{B} S_{0}\left(x_{t}\right) f_{B_{s}}^{2} B_{s}\left|V_{t s} V_{t b}^{*}\right|^{2}$
The point is:

Very weak dependence on $\rho$ and $\eta$

$$
f_{B_{s}}^{2} B_{s}=\frac{f_{B_{s}}^{2} B_{s}}{f_{B_{s}}^{2} B_{d}} f_{B_{d}}^{2} B_{d}=\xi^{2} f_{B_{d}}^{2} B_{d}
$$

$\xi: S U(3)$-breaking corrections

Measurement of $\Delta m_{s}$ reduces the uncertainties on $f^{2}{ }_{B_{d}} B_{d}$ since $\xi$ is better known from Lattice QCD

$$
\sigma_{\text {rel }}\left(f_{\delta_{d / s}}^{2} B_{d / s}\right)=36 \% \rightarrow \quad \sigma_{\text {re }}\left(\xi^{2}=f_{\varepsilon_{i}}^{2} B_{s} \mid f_{s_{d}}^{2} B_{d}\right)=10 \%
$$

$\rightarrow$ Leads to improvement of the constraint from $\Delta \mathrm{m}_{\mathrm{d}}$ measurement on $\left|\mathrm{V}_{\mathrm{td}} \mathrm{V}_{\mathrm{tb}}^{*}\right|^{2}$

$$
\Delta m_{d}=\frac{G_{F}^{2}}{6 \pi^{2}} m_{B_{d}} m_{W}^{2} \eta_{B} S_{0}\left(x_{t}\right) f_{B_{d}}^{2} B_{d}\left|V_{t d} V_{t b}^{*}\right|^{2} \propto A^{2} \lambda^{6}\left[(1-\bar{\rho})^{2}+\bar{\eta}^{2}\right]
$$

## $\Delta \mathrm{m}_{\mathrm{s}}$



The signal has a significance of $5.4 \sigma$

## Constraint on $\left|V_{\mathrm{td}} / V_{\mathrm{ts}}\right|$

$\frac{\Delta m_{d}}{\Delta m_{s}}=\frac{m_{B d}}{m_{B s}} \xi_{\Delta m}^{-2} \frac{\left|V_{t d}\right|^{2}}{\left|V_{t s}\right|^{2}}$
$\rightarrow$ First strongindication that $B_{s}-B_{s}$ mixing is probably SMlike.


## Putting it all together



Inputs:

$$
\begin{gathered}
\left|\frac{V_{u b}}{V_{c b}}\right| \\
\Delta m_{d} \\
\Delta m_{s} \\
B \rightarrow \tau v \\
\left|\varepsilon_{K}\right|
\end{gathered}
$$

$\sin 2 \beta$

## LHCb physics

- It is time to calculate $B_{s}$ decays
- Yu, Li, Lu 05, 06
- Xiao, Chen, Guo 06; Xiao, Liu, Wang 06
- Wu, Zhong, Zuo 06


## Polarization in $\mathrm{B} \rightarrow \mathrm{VV}$

- Many works from Lu's group using PQCD

| Decay | Branching ratio |  | polarization fraction $R_{L}(\%)$ |  |  | $R_{\\|}(\%)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | theory | exp. | theory | exp. |  |  |
| $B^{0} \rightarrow \rho^{-} K^{*+}$ | $10-13$ | $\leq 24$ | $71-78$ |  | 12 | 10 |
| $B^{+} \rightarrow \rho^{+} K^{* 0}$ | $13-17$ | $10.5 \pm 1.8$ | $76-82$ | $66 \pm 7$ | 13 | 10 |
| $B^{+} \rightarrow \rho^{0} K^{*+}$ | $6-9$ | $10.6_{-3.5}^{+3.8}$ | $78-85$ | $96_{-15}^{+4} \pm 4$ | 11 | 11 |
| $B^{+} \rightarrow \omega K^{*+}$ | $5-8$ | $<7.4$ | $73-81$ |  | 19 | 9 |
| $B^{0} \rightarrow \rho^{+} \rho^{-}$ | $35 \pm 5 \pm 4$ | $30 \pm 6$ | 94 | $96_{-7}^{+4}$ | 3 | 3 |
| $B^{+} \rightarrow \rho^{+} \rho^{0}$ | $17 \pm 2 \pm 1$ | $26.4_{-6.4}^{+6.1}$ | 94 | $99 \pm 5$ | 4 | 2 |
| $B^{+} \rightarrow \rho^{+} \omega$ | $19 \pm 2 \pm 1$ | $12.6_{-3.8}^{+4.1}$ | 97 | $88_{-15}^{+12}$ | 1.5 | 1.5 |
| $B^{0} \rightarrow \rho^{0} \rho^{0}$ | $0.9 \pm 0.1 \pm 0.1$ | $<1.1$ | 60 | - | 22 | 18 |
| $B^{0} \rightarrow \rho^{0} \omega$ | $1.9 \pm 0.2 \pm 0.2$ | $<3.3$ | 87 | - | 6.5 | 6.5 |
| $B^{0} \rightarrow \omega \omega$ | $1.2 \pm 0.2 \pm 0.2$ | $<19$ | 82 | - | 9 | 9 |

## Conclusion

- Great progress in theoretical and experimental studies of B physics has been made.
- Discrepancies have appeared, but are not significant enough for new physics discovery.
- Continuous effort is required.

